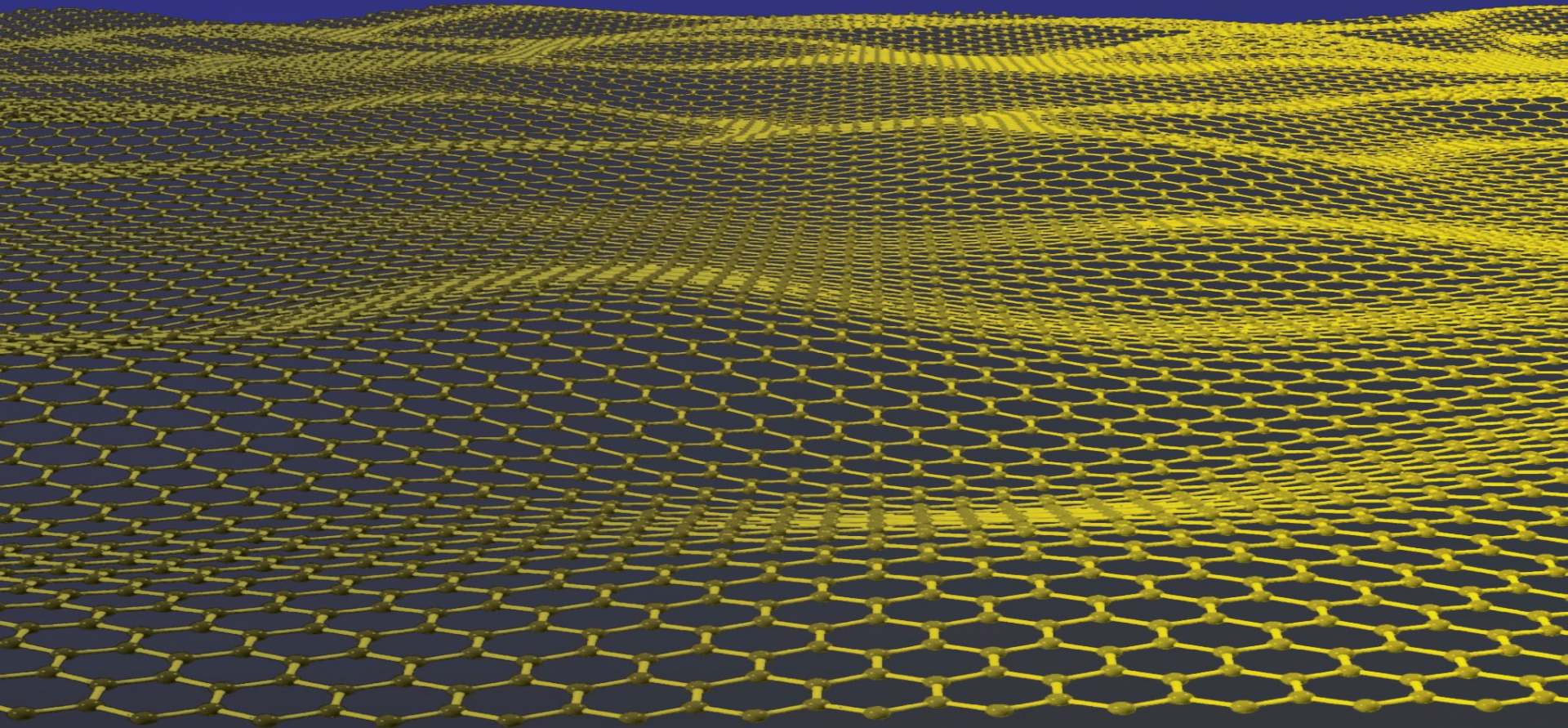


Graphene

and numerical simulations



Nonrelativistic particle

$$E = \frac{mv^2}{2}$$

Relativistic particle

$$E = \sqrt{m^2 c^4 + p^2 c^2}$$

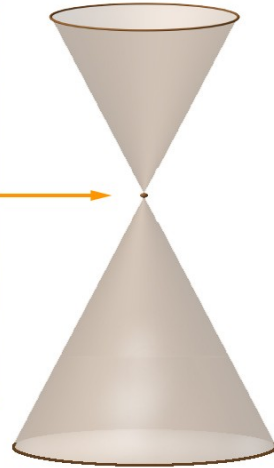
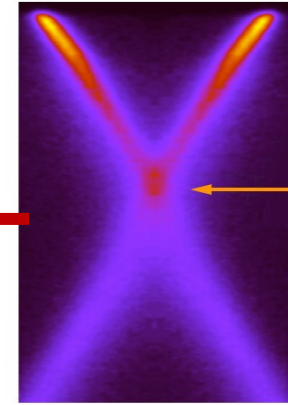
Relativistic particle $E = \sqrt{m^2 c^4 + p^2 c^2}$

Massless particle $E = cp$

Relativistic particle $E = \sqrt{m^2 c^4 + p^2 c^2}$

Massless particle $E = cp$

Graphene $E = v_F p$, $v_F = \frac{c}{300}$;



Dirac bispinor!

1

**Two dimensional Dirac particles,
interacting via 3D Coulomb**

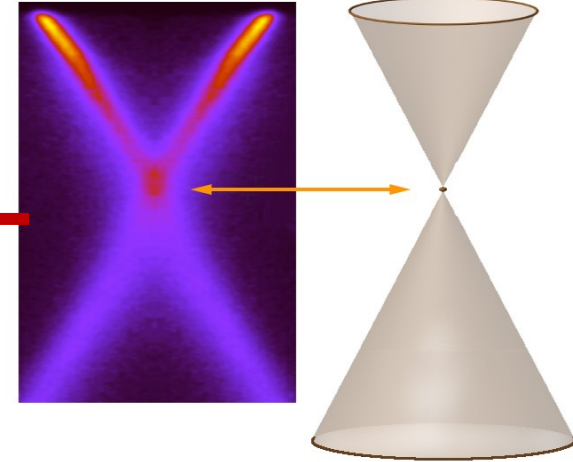
Relativistic particle $E = \sqrt{m^2 c^4 + p^2 c^2}$

Massless particle $E = cp$

Graphene $E = v_F p$; $v_F = \frac{c}{300}$;

$$\alpha_g = 300\alpha = 2.16 > 1$$

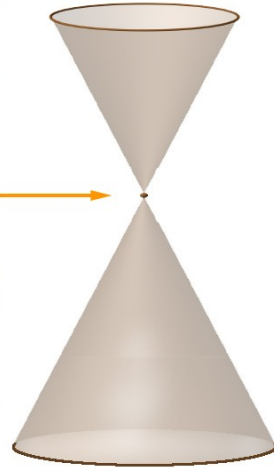
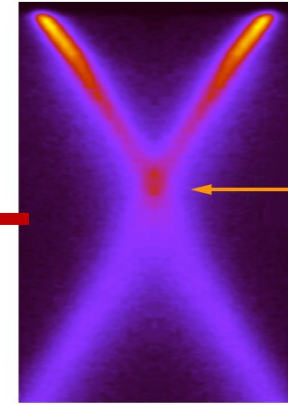
$\alpha_g > \alpha_g^{crit} = 1.11 \pm 0.06$ Pure graphene is the insulator!



Relativistic particle $E = \sqrt{m^2 c^4 + p^2 c^2}$

Massless particle $E = cp$

Graphene $E = v_F p$; $v_F = \frac{c}{300}$;



$$\alpha_g = 300\alpha = 2.16 > 1$$

$\alpha_g > \alpha_g^{crit} = 1.11 \pm 0.06$ Pure graphene is the insulator!

If we put graphene on a substrate we can get conductor: $\alpha_g \rightarrow \frac{2}{1 + \epsilon} \alpha_g$

Numerical calculation of α_g^{crit}

2

Is graphene in vacuum an insulator?.

Joaquin E. Drut Timo A. Lahde

e-Print: [arXiv:0807.0834](https://arxiv.org/abs/0807.0834) [cond-mat.str-el],
PRL (2009)

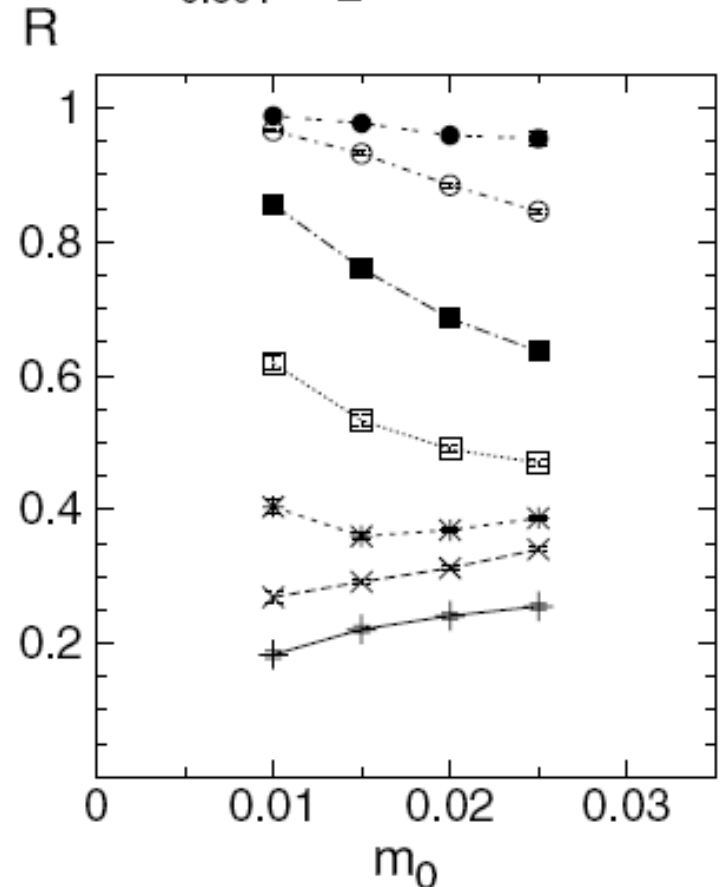
Monte Carlo Simulation of the Semimetal-Insulator
Phase Transition in Monolayer Graphene.

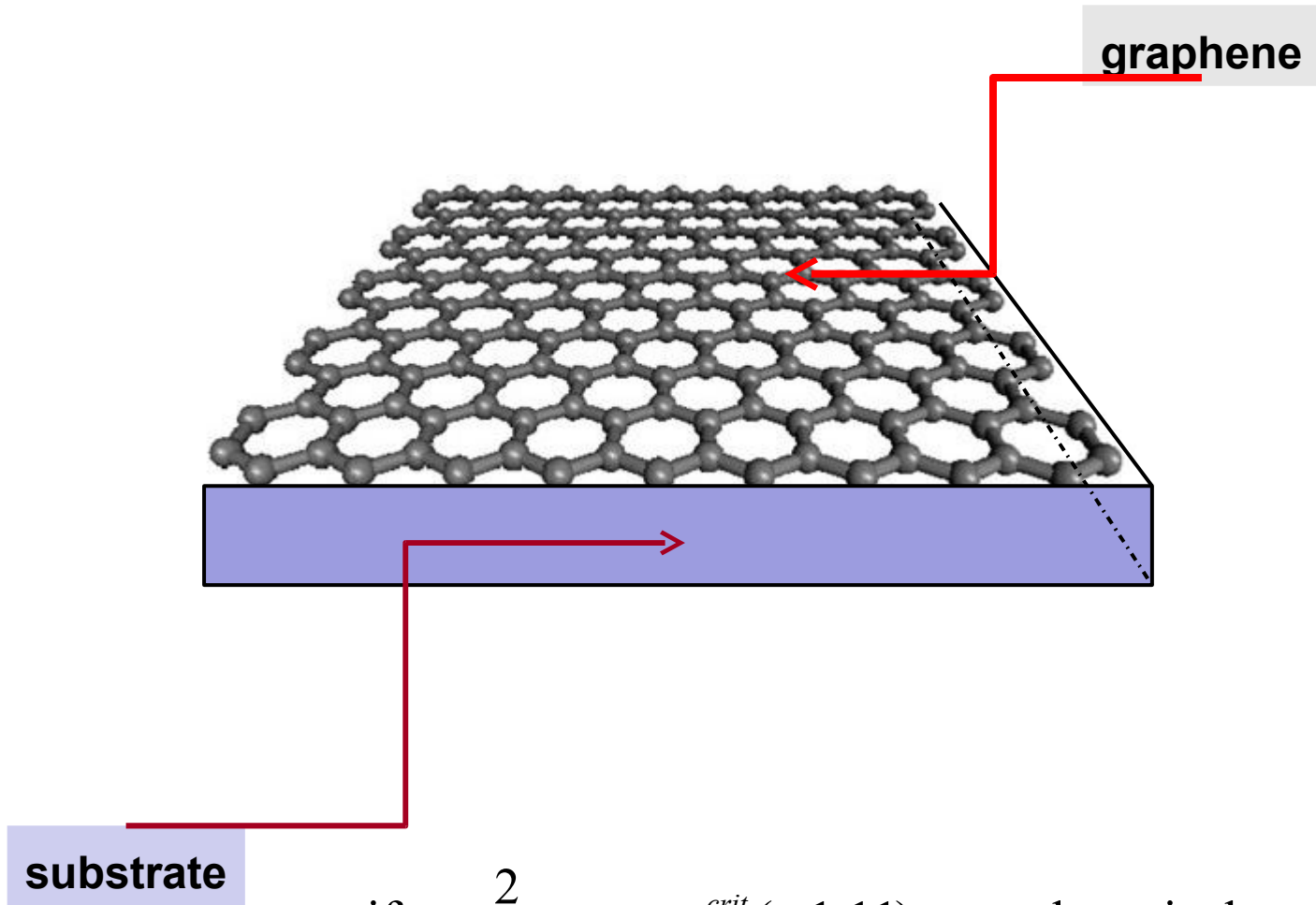
W. Armour , Simon Hands, Costas Strouthos

Published in **Phys.Rev. B81 (2010) 125105**

e-Print: [arXiv:0910.5646](https://arxiv.org/abs/0910.5646) [cond-mat.str-el]

$N_f = 2, \beta = 0.050$ —+—+— 0.111 —■—
 0.067 —x—x—x— 0.143 —○—○—
 0.077 —*—*—*— 0.200 —●—●—
 0.091 —□—□—□—

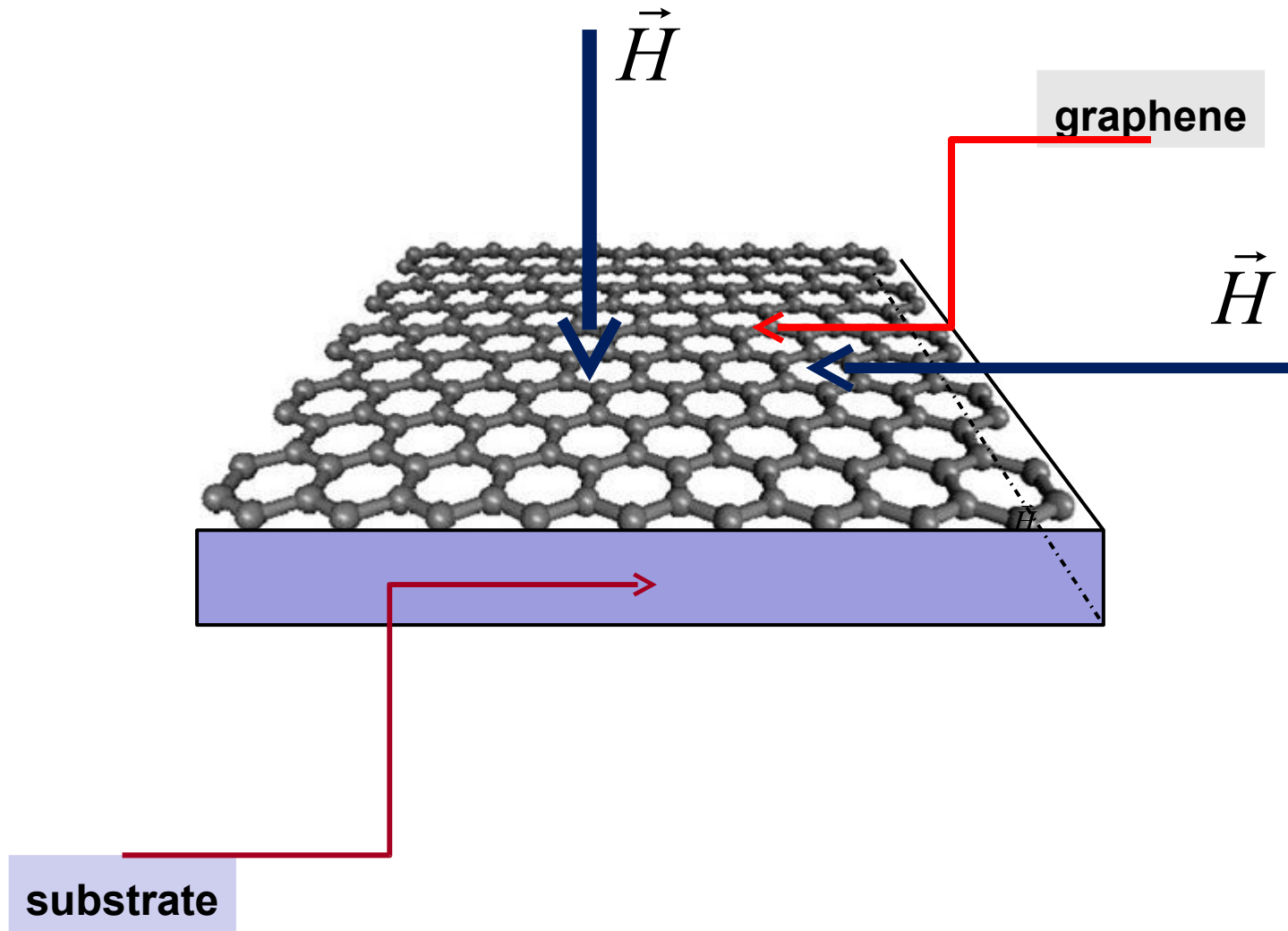




if $\frac{2}{1+\epsilon}\alpha_g > \alpha_g^{crit} (= 1.11)$ graphene is the conductor

We can numerically simulate conductor – insulator phase transition!

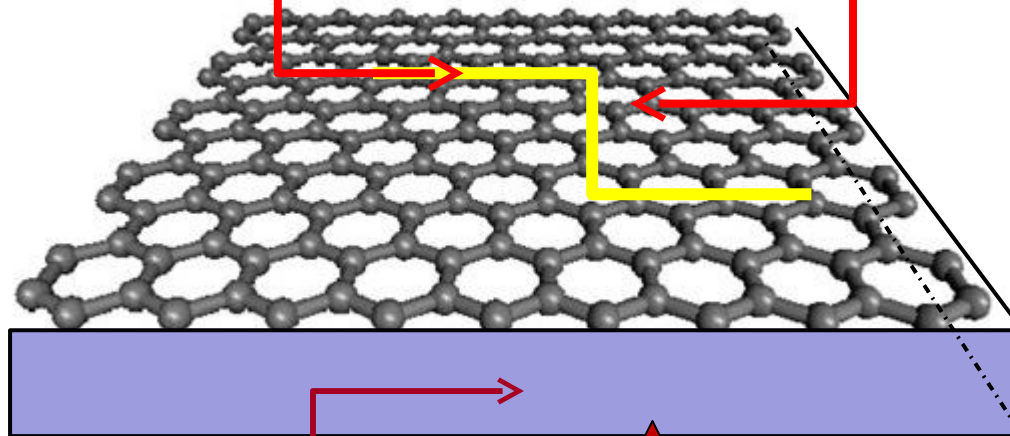
Magnetic Field and Graphene



Graphene changes its properties when an external magnetic field is applied, we can numerically simulate all that

Trajectory of the magnetic head

graphene



3

Ferromagnetic substrate

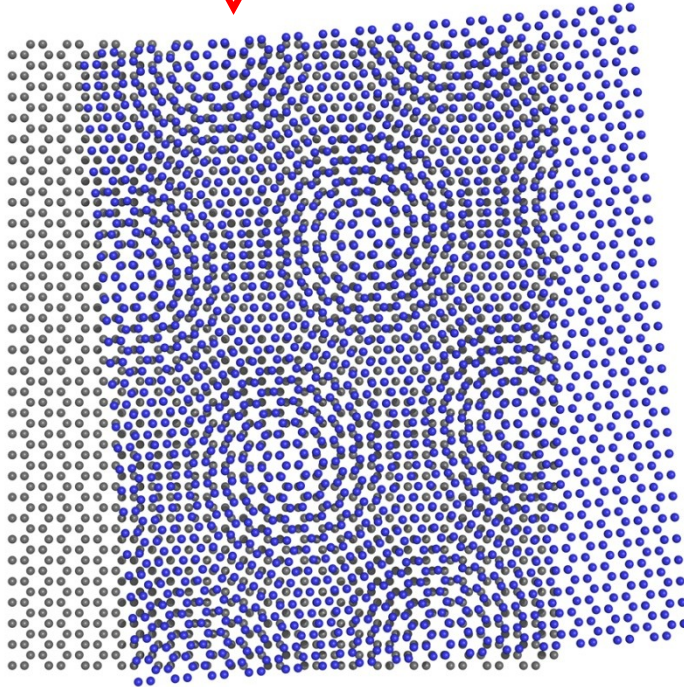
magnetic head

Along the trajectory of the magnetic head graphene becomes the conductor!

We can draw (construct) chips! All that we can simulate on computers

Problems for graphene numerical simulations

Magnetic field
Finite temperature
Impurities
2-3-4 layers
Conductivity
Viscosity – Entropy
Optical properties
Critical indices

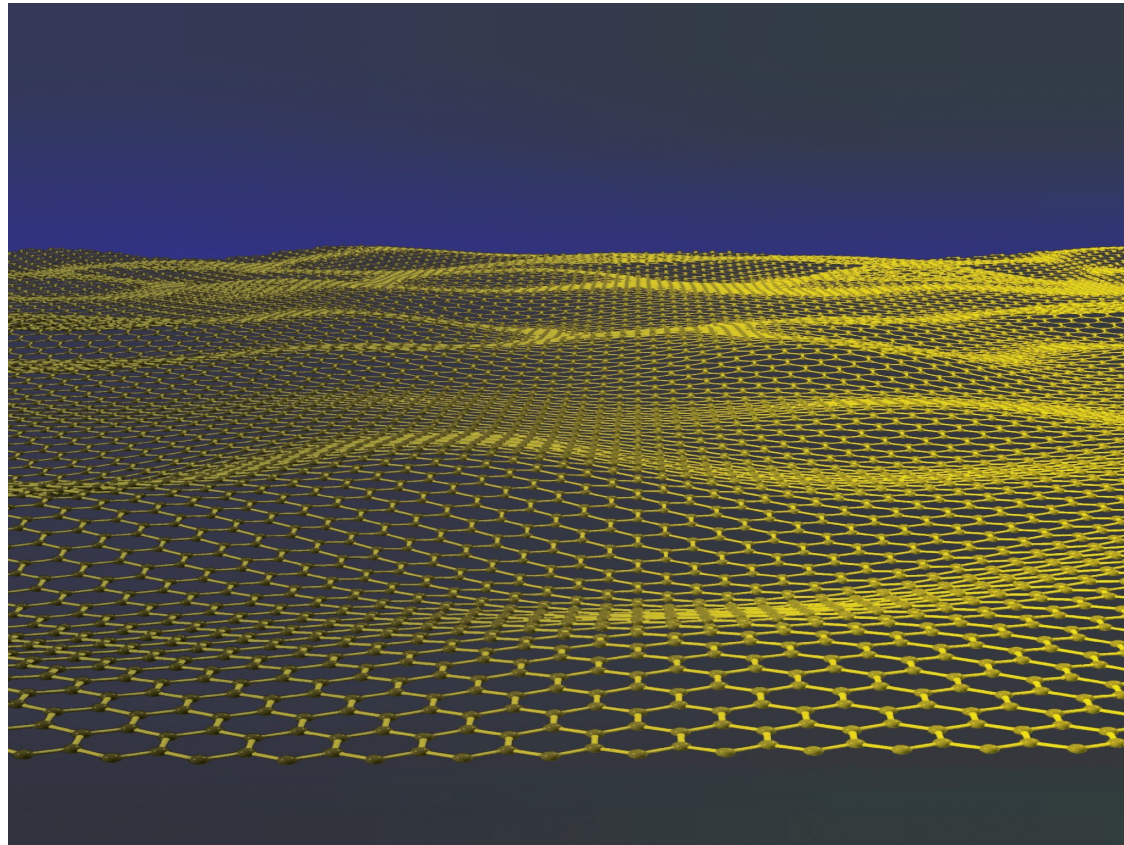


Monte Carlo simulation of monolayer graphene at non-zero temperature

Wesley Armour^{a,b}, Simon Hands^c, and Costas Strouthos^d

arXiv:1105.1043v1 [cond-mat.str-el] 5 May 2011

**Curvature of the graphene leads to two dimensional gravity for fermions
Volovik**



Graphene simulations

High Temperature Superconductor

simulations

6